

# ***Analytical calculation of encapsulation-induced variation of PV modules efficiency***

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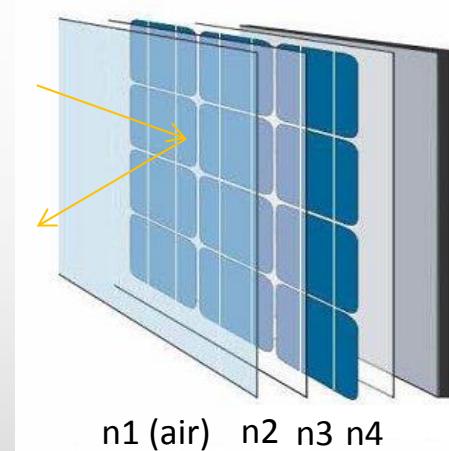
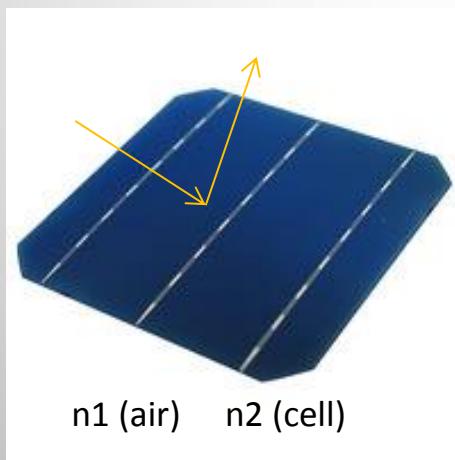
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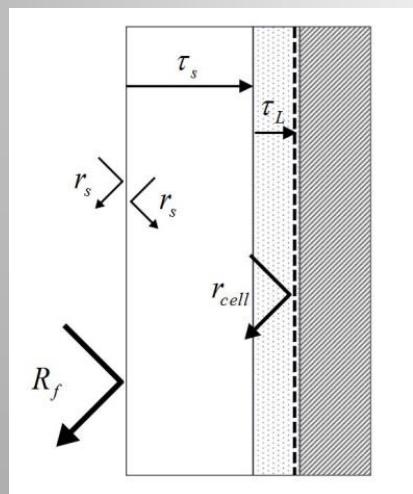
- Multiple encapsulation configurations can be conceived in the design phase of PV modules (specially BIPV modules).
- Evaluation of performance of encapsulation materials in terms of their effect on module efficiency is required.
- Manufacturing and experimental characterization of every possible combination (superstrate and polymer interlayer types, thickness, colour, etc.) is costly and time demanding.

- Short-circuit current density is directly related with spectral absorptivity of the PV cells in encapsulated conditions.
- Absorptivity of encapsulated PV cells is not accessible from spectrophotometry. Calculation needed.



## Calculation of layer-by-layer absorption in a PV module

- Literature: numerical ray-tracing, multidirectional numerical net radiation methods, etc.
- This work: separation in optical components, each of them defined through a transfer matrix connecting energy fluxes.



### Optical model:

T. Baenas, M. Machado, Solar Energy 125 (2016) 256 – 266

<http://authors.elsevier.com/a/1SKRE,tRcw4aW>

- The reflectivity of the cell,  $r_{cell}$ , is introduced through a virtual opaque coating component.
- Singular solution to the equation system for the energy coefficients of the optical system:

$$r_{cell} = \frac{R_f - r_s}{\tau_s^2 \tau_L^2 (1 - 2r_s + R_f r_s)}$$

- $R_f, r_s, \tau_s, \tau_L$  are obtained from spectrophotometry and well-known, standardized calculations (EN 410).
- Once determined,  $r_{cell}$  may be applied to any other config.

- The model also provides simple analytical expressions for layer-by-layer absorptance:

$$A_{mod} = (1 - r_s) \frac{1 - r_{cell} \tau_s^2 \tau_L^2}{1 - r_s r_{cell} \tau_s^2 \tau_L^2},$$

$$A_{cell} = (1 - r_s)(1 - r_{cell}) \frac{\tau_s \tau_L}{1 - r_s r_{cell} \tau_s^2 \tau_L^2},$$

$$A_{enc} = (1 - r_s) (1 - \tau_s \tau_L) \frac{1 + \tau_s \tau_L r_{cell}}{1 - r_s r_{cell} \tau_s^2 \tau_L^2},$$

$$A_{mod} = 1 - R_f = A_{cell} + A_{enc}$$

## Relationship between $A_{cell}$ and short-circuit current

Short-circuit current of a bare cell

$$J_{sc, \text{bare}} = q \int_{\lambda_1}^{\lambda_2} \phi(\lambda) EQE_{\text{bare}}(\lambda) d\lambda$$

Short-circuit current encapsulated cell

$$J_{sc, \text{mod}} = q \int_{\lambda_1}^{\lambda_2} \phi(\lambda) EQE_{\text{mod}}(\lambda) d\lambda$$

$$IQE_{\text{mod}}(\lambda) = \frac{EQE_{\text{mod}}(\lambda)}{A_{\text{cell}}(\lambda)}$$

$A_{\text{cell}}$  ≡ Encapsulated cell absorptivity

- IQE of a bare cell is easily determined from air-cell spectral response and reflectance measurements.
- It is assumed here that this magnitude is intrinsic to the cell, so that,

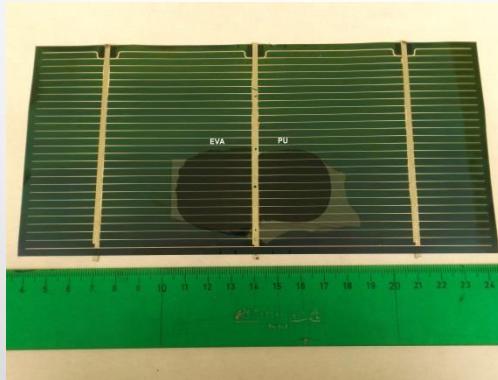
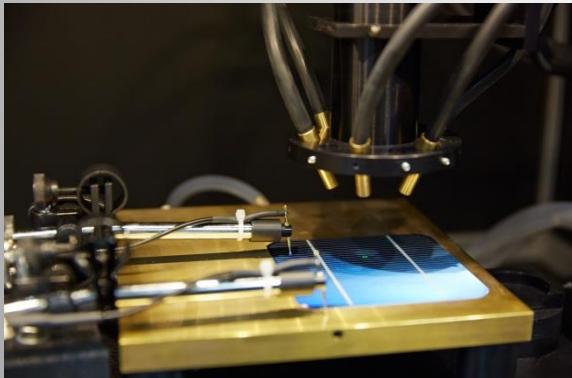
$$IQE_{bare}(\lambda) = IQE_{mod}(\lambda)$$

Short-circuit current of encapsulated cell

$$J_{sc, mod} = q \int_{\lambda_1}^{\lambda_2} \phi(\lambda) IQE_{bare}(\lambda) A_{cell}(\lambda) d\lambda$$

## Experimental validation: short-circuit current

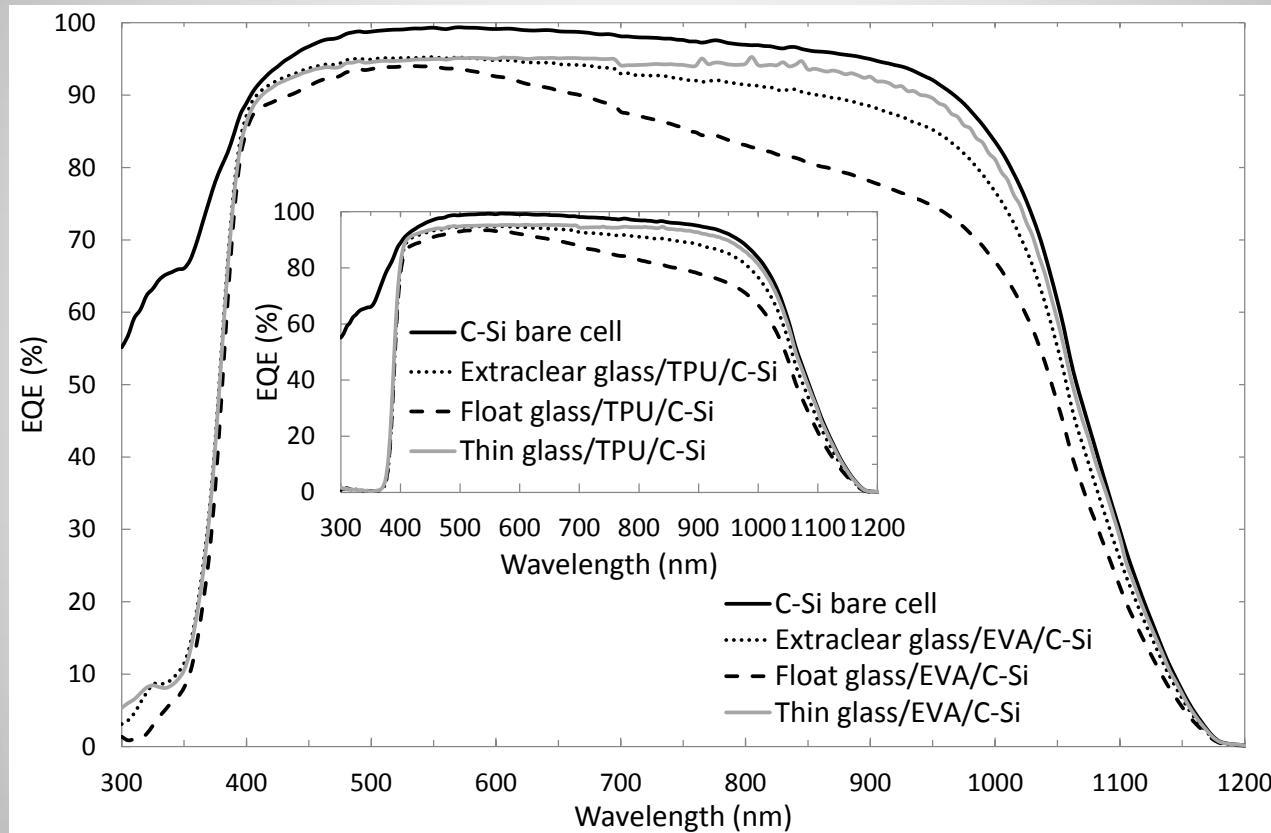
- Experimental and calculated short-circuit current for 12 encapsulation configurations have been compared.
- All combinations of commercial c-Si and CIGS cells with extraclear, float and thin glass superstrates, EVA and TPU encapsulation materials tested.



Experimental validation

M. Machado et al.,  
submitted to Solar Energy Mat. and Solar Cells

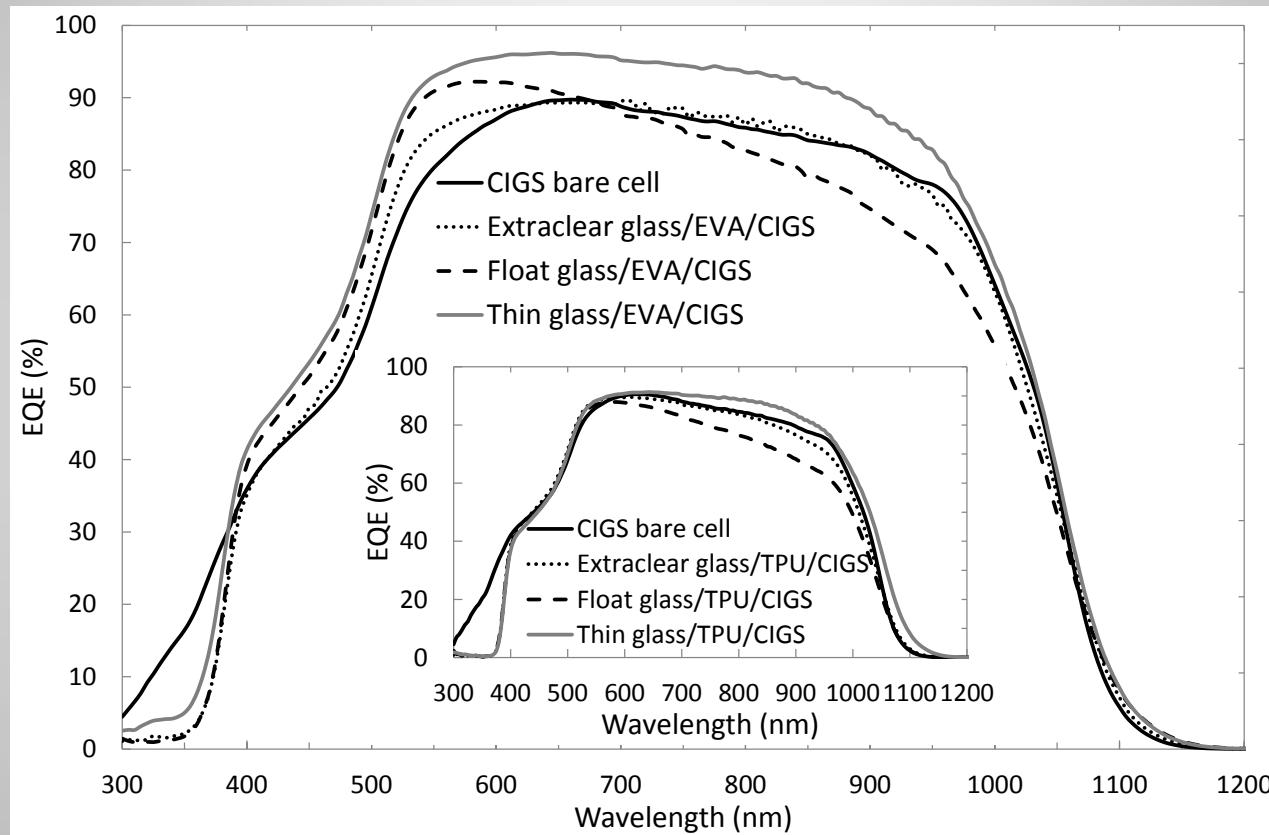
# Experimental External Quantum Efficiency- Silicon cell



Experimental validation

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submitted to Solar Energy Mat. and Solar Cells

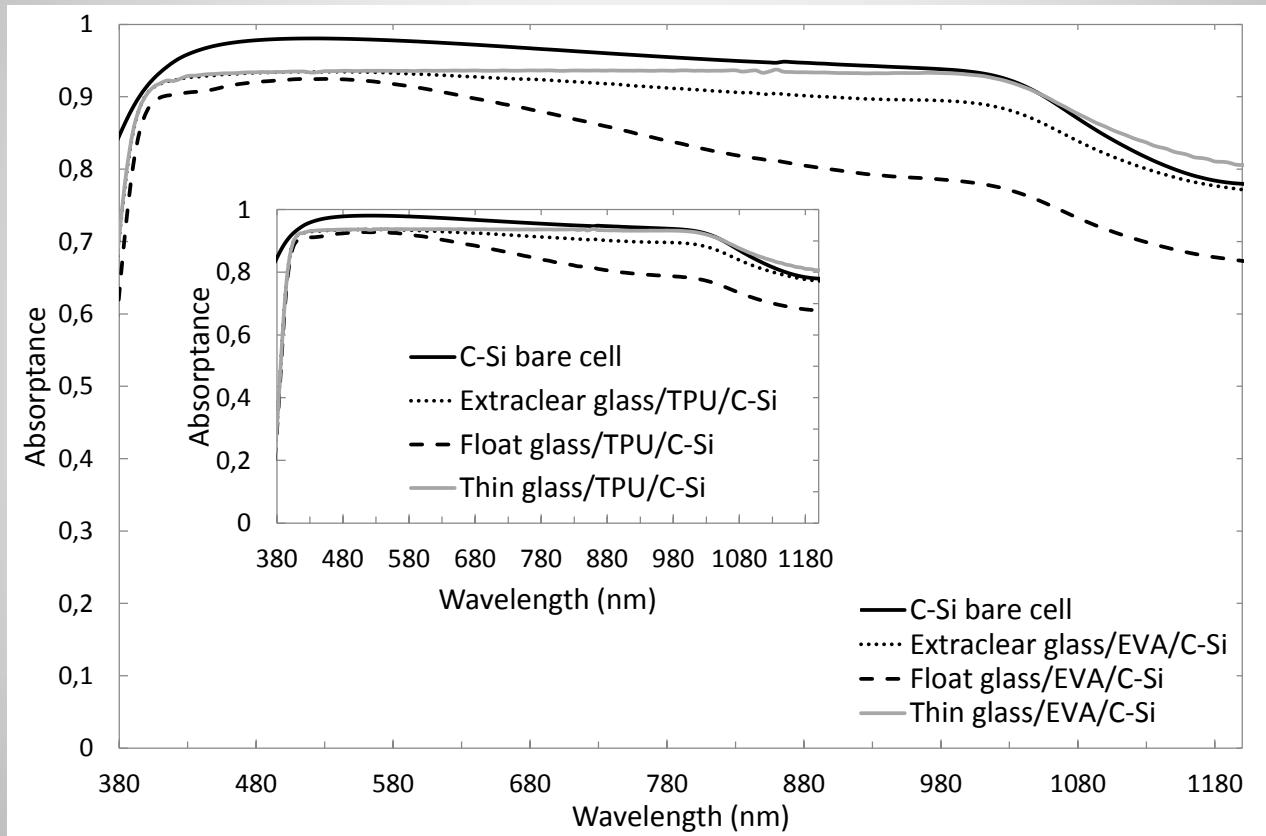
# Experimental External Quantum Efficiency- CIGS cell



Experimental validation

M. Machado et al.,  
submitted to Solar Energy Mat. and Solar Cells

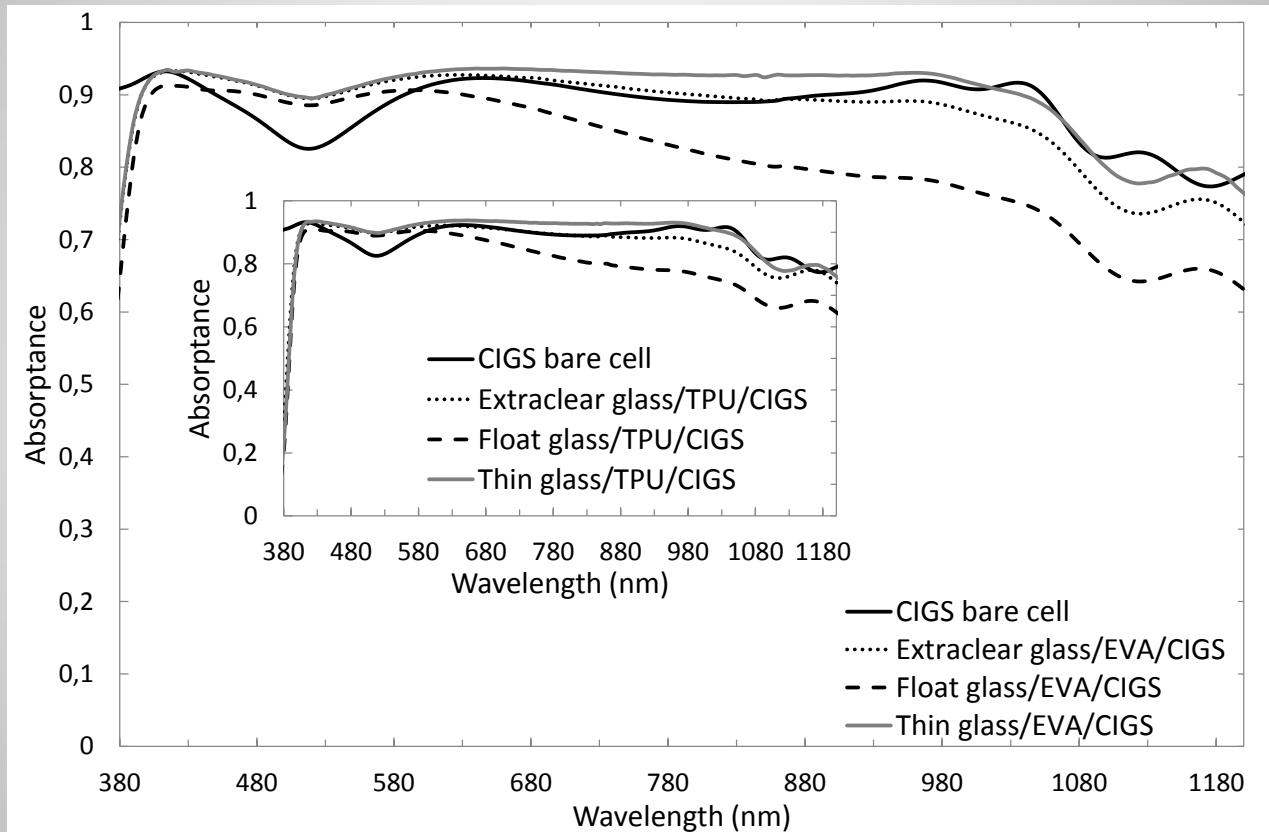
# Calculated absorptance of encapsulated Silicon cell



Experimental validation

M. Machado et al.,  
submitted to Solar Energy Mat. and Solar Cells

# Calculated absorptance of encapsulated CIGS cell



Experimental validation

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# Calculated vs experimental short-circuit values

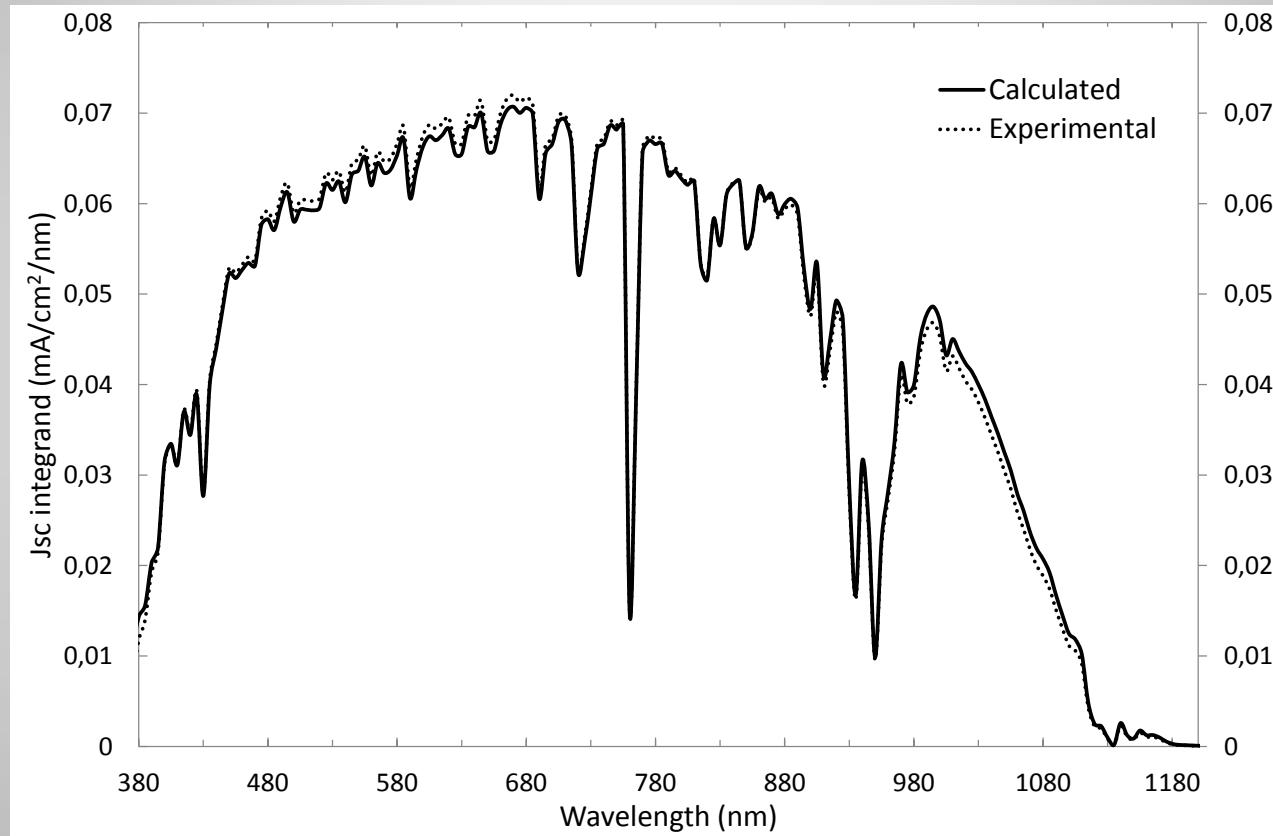
Silicon cells      CIGS cells

Encapsulation configuration	$J_{sc}$ calc. (mA/cm <sup>2</sup> )	$J_{sc}$ exp. (mA/cm <sup>2</sup> )	$\Delta J_{sc}$ total (mA/cm <sup>2</sup> )	Error (%)
Extraclear glass/EVA/Si cell	37.3	37.2	0.1	0.2
Float glass/EVA/Si cell	35.0	34.8	0.2	0.6
Thin glass/EVA/Si cell	38.0	38.0	0.0	0.0
Extraclear glass/TPU/Si cell	37.1	36.8	0.3	0.8
Float glass/TPU/Si cell	34.9	34.4	0.5	1.5
Thin glass/TPU/Si cell	37.9	37.9	0.0	0.0
Encapsulation configuration	$J_{sc}$ calc. (mA/cm <sup>2</sup> )	$J_{sc}$ exp. (mA/cm <sup>2</sup> )	$\Delta J_{sc}$ total (mA/cm <sup>2</sup> )	Error (%)
Extraclear glass/EVA/CIGS cell	31.3	31.3	0.0	0.0
Float glass/EVA/CIGS cell	29.4	29.4	0.0	0.0
Thin glass/EVA/CIGS cell	31.8	32.2	-0.4	-1.3
Extraclear glass/TPU/CIGS cell	30.9	30.5	0.4	1.4
Float glass/TPU/CIGS cell	29.1	28.7	0.4	1.2
Thin glass/TPU/CIGS cell	31.8	32.2	-0.4	-1.1

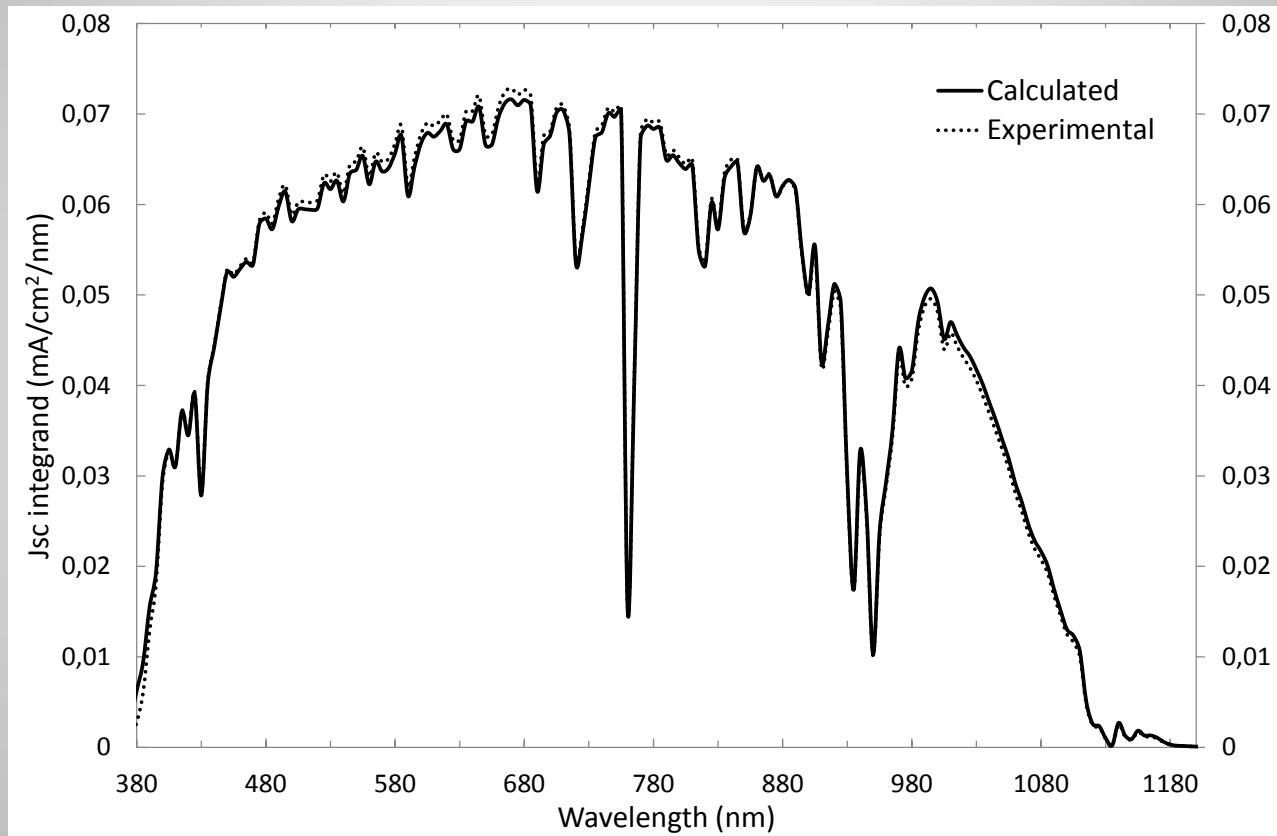
## Experimental validation

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## Spectral comparison, extraclear glass/EVA/Si cell



## Spectral comparison, ultrathin glass/TPU/Si cell



## Conclusions

- Transfer matrix method applied to deduce analytical expressions for encapsulated solar cells absorptivity.
- Simple method to evaluate the influence of encapsulation materials on cell efficiency.
- The experimental determination of a single configuration allows the prediction of multiple other configurations in terms of short-circuit currents.
- Very good agreement shown between theoretical calculation and experimental measurements.

# Thank you for your attention

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